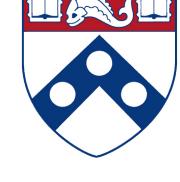
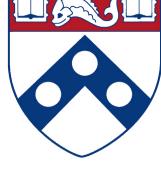


# A graph-theoretic approach to neuroimaging experimental design



Geoffrey K. Aguirre

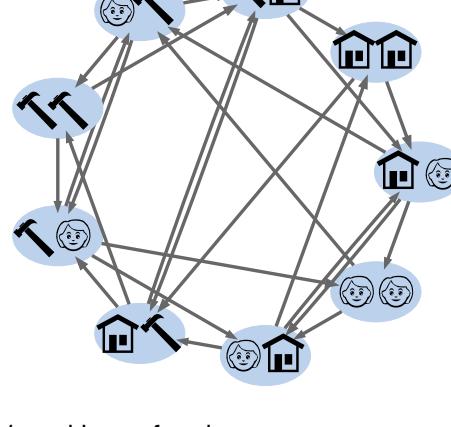
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- Stimulus counterbalance is critical for experimental design
- A graph-theoretic approach considers stimuli (or the transitions between them) as nodes within a graph
- The Hamiltonian cycle yields a counterbalanced sequence (de Bruijn cycle)
- Mathematical optimization methods (e.g., simulated annealing) may be used to select paths that have desirable properties, for example:
  - low discrepancy (high uniformity)
  - modulation at frequencies detectable by BOLD fMRI

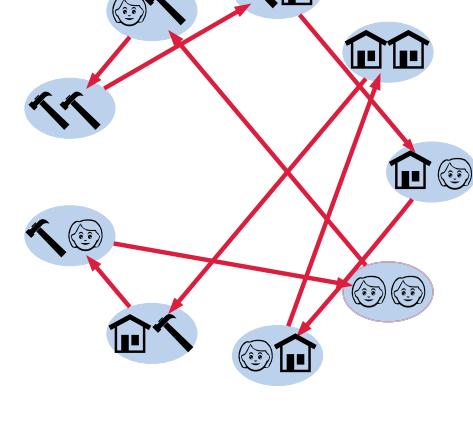
a. Three categories of stimuli; how to counterbalance?



b.  $k=3, n=2$ , de Bruijn graph



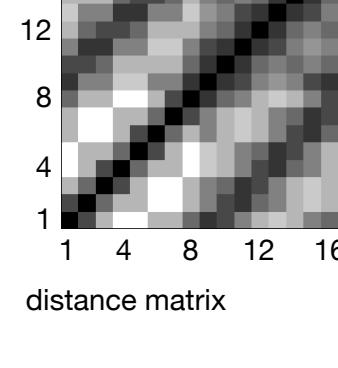
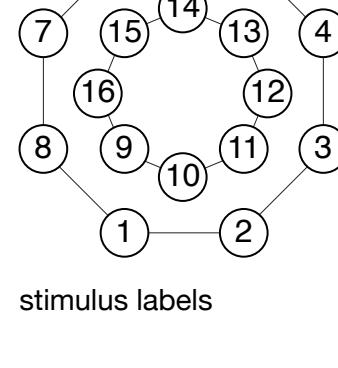
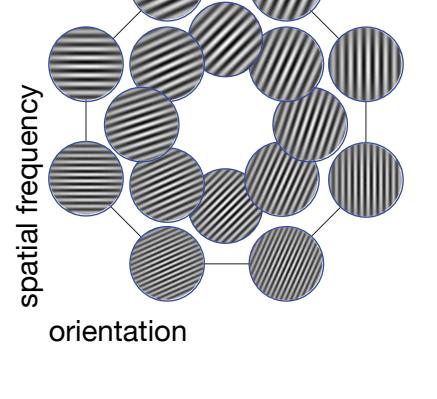
c. Hamiltonian cycle



d. necklace of nodes

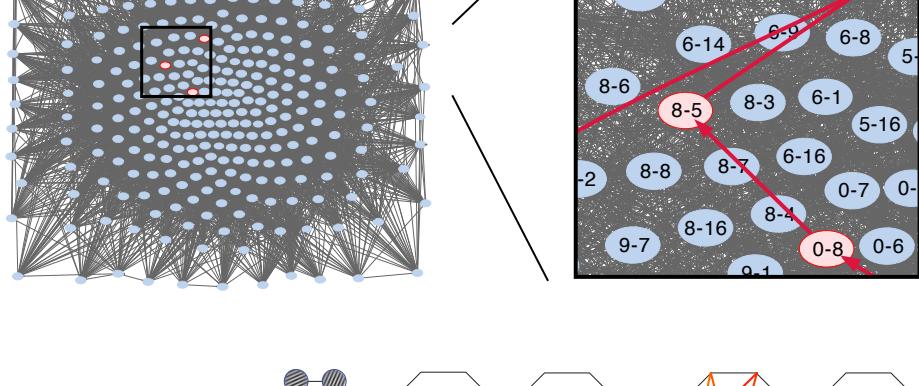


e. de Bruijn cycle



## Temporal positioning of neural modulation

### 1st order counterbalancing ( $n=2$ )



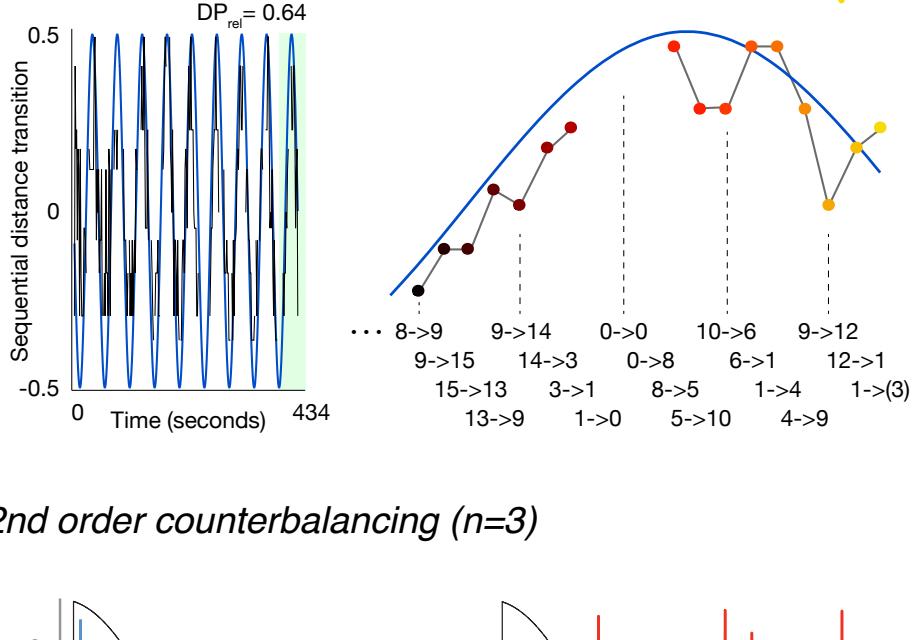
## Minimizing discrepancy for MVPA studies

### Design goals:

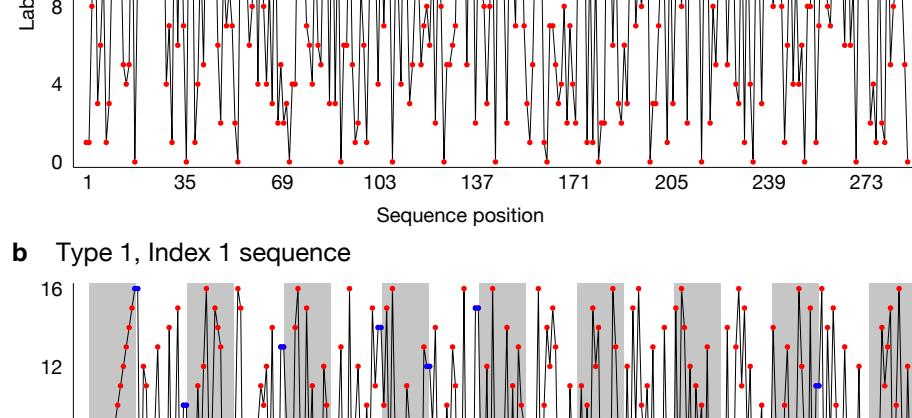
- maximize responses vs. null condition
- uniform (minimal discrepancy) distribution of events to optimize prediction
- 1st order counterbalance to minimize / remove carry-over effects

### T1I1 sequences minimize discrepancy

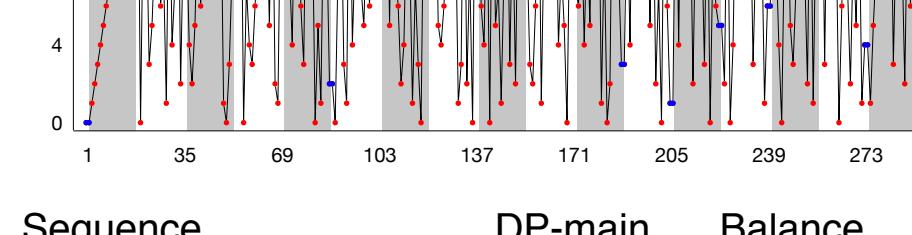
a de Bruijn cycle prohibited from returning to a label node prior to exhausting labels



### a M-sequence



### b Type 1, Index 1 sequence



Sequence	DP-main	Balance
n=2	Random de Bruijn	0.34
	M-sequence	0.32
	T1I1	0.34
n=3	M-sequence	0.05
	Optimized de Bruijn	0.32

Balance is a measure of the even distribution of labels across the sequence; small numbers indicate more balance (Y Hsieh et al. 2004. Ars Combinatoria, 72, 277–286)

Download software from:  
<http://cfn.upenn.edu/aguirre>



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GK Aguirre, MG Mattar, L Magis-Weinberg.  
 (2011) de Bruijn cycles for neural decoding.  
*NeuroImage* 56: 1293-1300

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